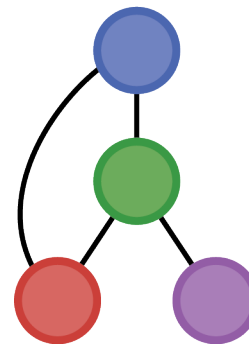


Robust Design of Controlled Environment Agriculture Systems for Venture Investment Decision-Making

Dimitri Alston, Alireza Miraliakbar, Nia Samuels
Matthew Stuber, P&W Associate Professor in
Advanced Systems Engineering

November 6th, 2025

2025 / AICHE
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MEETING

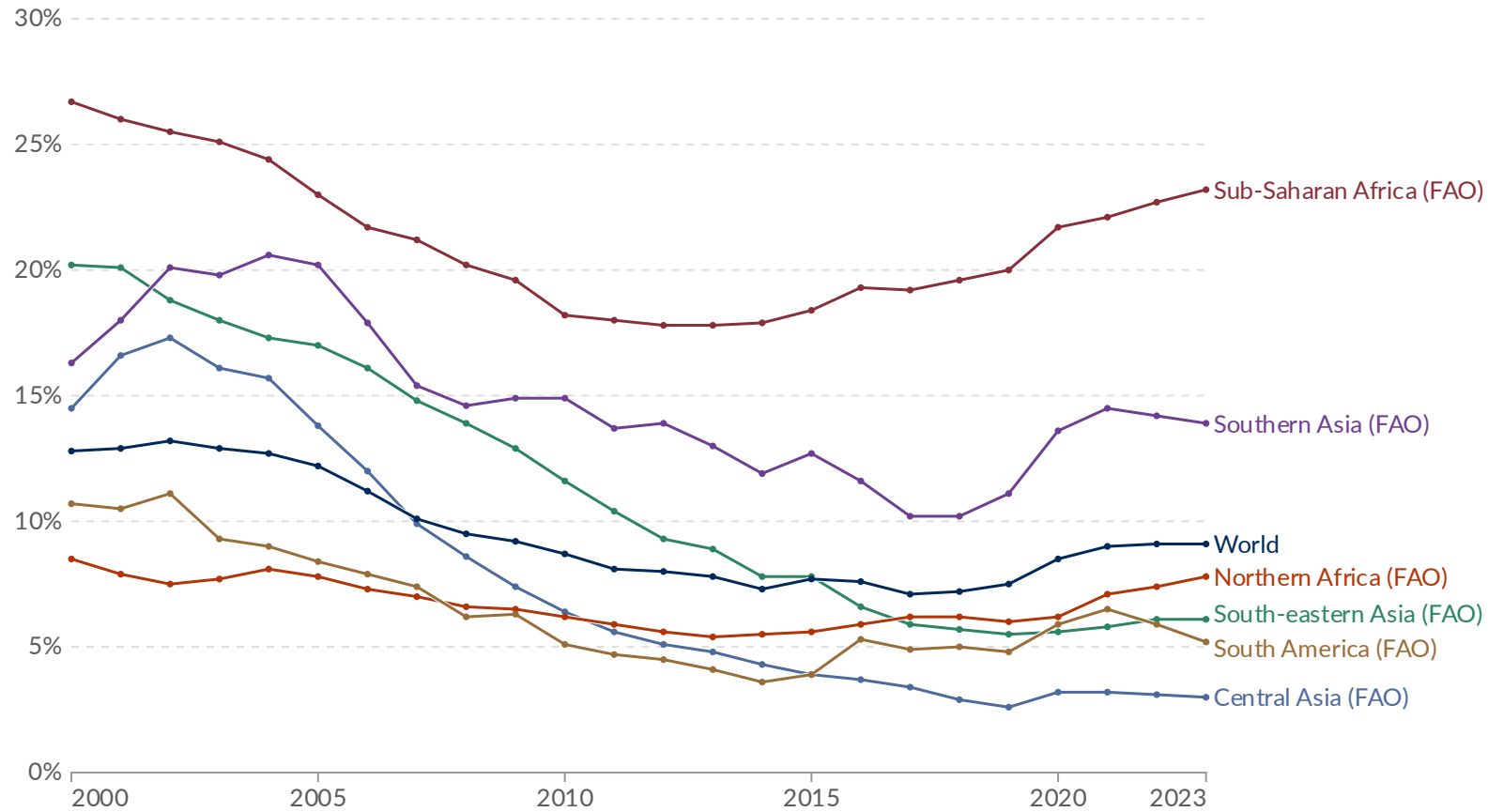


Process Systems and
Operations Research
Laboratory

Introduction

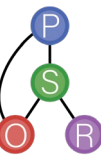
Share of people who are undernourished

Our World
in Data



[1] Ritchie, H. Rosado, P and Roser, M. "Hunger and Undernourishment" Published online at OurWorldinData.org. (2023) Retrieved from: '<https://ourworldindata.org/hunger-and-undernourishment>'

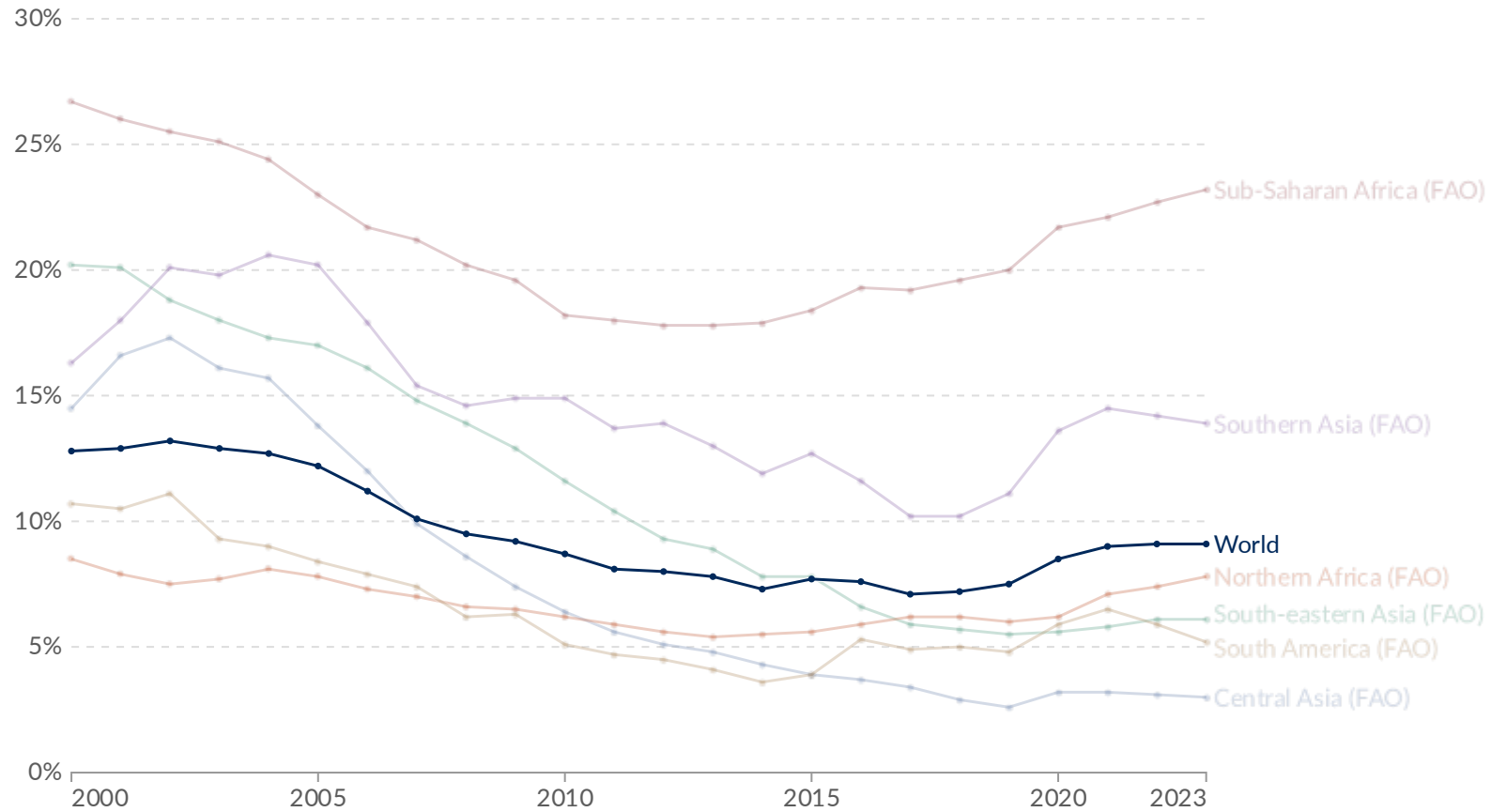
AIChE Annual Meeting 2025



Introduction

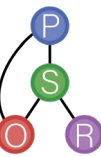
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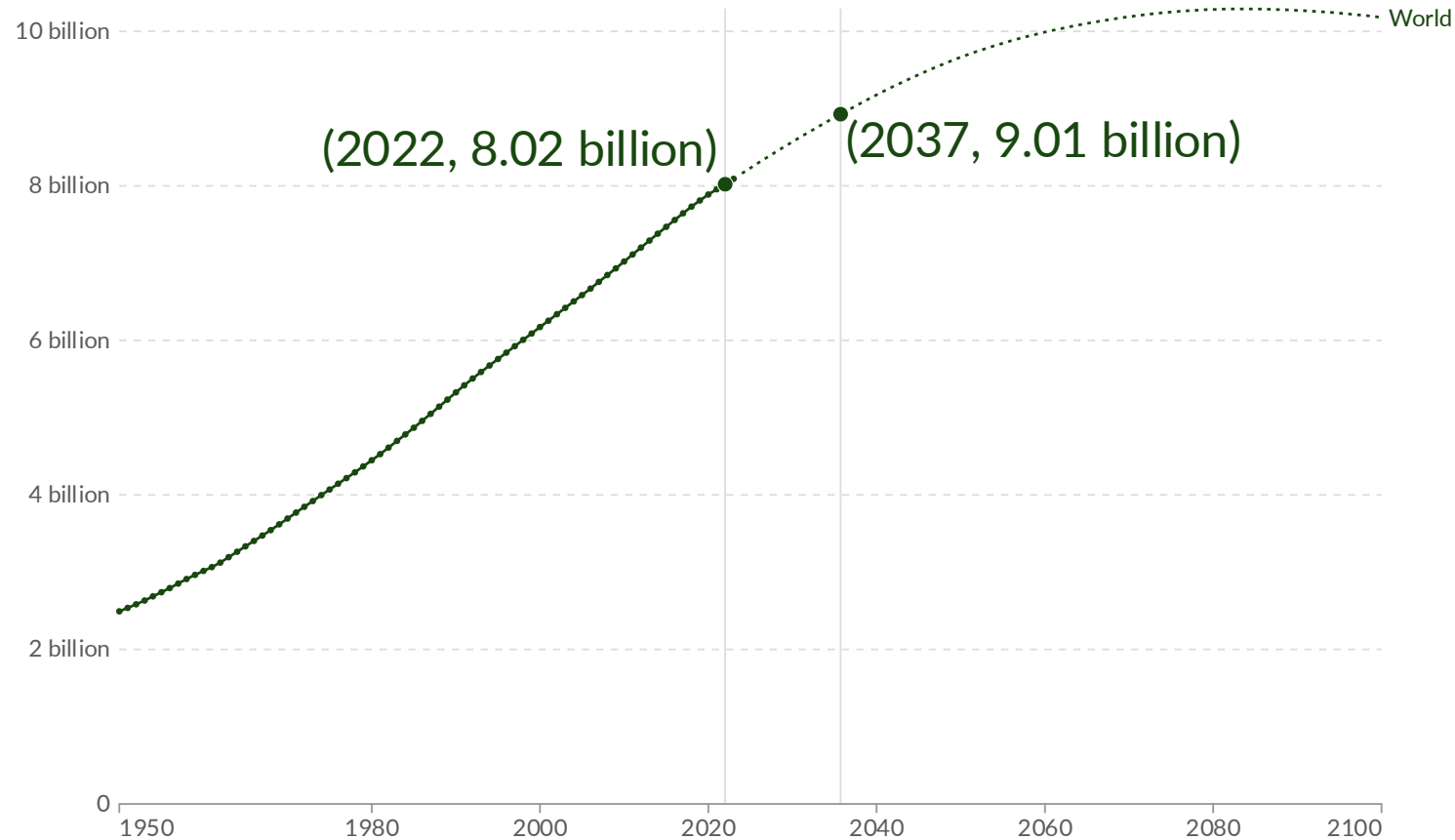
AICHe Annual Meeting 2025



Introduction

Population, 1950 to 2100

Our World
in Data



[2] Ritchie, H. et. al. "Population Growth" Published online at OurWorldinData.org. (2023) Retrieved from: '<https://ourworldindata.org/population-growth>'

AIChE Annual Meeting 2025



Introduction

Problem:

- Food insecurity is a rising issue^[3]
- Current agricultural practices are not enough

Solution:

- Controlled environment agriculture (CEA)



[3] Cetegen, S.A. and Stuber, M.D. Optimal design of controlled environment agricultural systems under market uncertainty. Computers & Chemical Engineering, 149:107285, 2021. ISSN 0098-1354.

[4] <https://amplifiedaginc.com/why-controlled-environment-agriculture-cea-is-mission-critical/>

Agricultural Practices

Traditional Methods



[5]

- Hindered by unpredictable environmental changes^[6]
- Contribute to climate change^[6]
- Use a significant amount of land^[6]
- Transportation spoilage^[6]

CEA Systems



[4]

- Climate controlled
 - Flexible location
-
- Have substantial operating costs^[3,7]
 - Venture risk^[3]

[3] Cetegen, S.A. and Stuber, M.D. Optimal design of controlled environment agricultural systems under market uncertainty. Computers & Chemical Engineering, 149:107285, 2021. ISSN 0098-1354.

[4] <https://amplifiedaginc.com/why-controlled-environment-agriculture-cea-is-mission-critical/>

[5] <https://www.dahu.bio/en/knowledge/agriculture/traditional-agriculture>

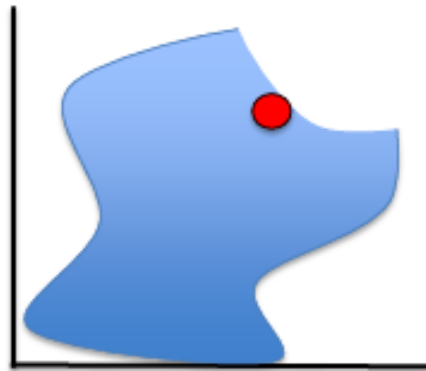
[6] Food and Agriculture Organization of the United Nations (FAO). The State of Agricultural Commodity Markets - Agricultural Trade, Climate Change, and Food Security. 2018.

[7] Calvo-Baltanás, V. et al. The future potential of controlled environment agriculture. PNAS Nexus, page 078, 03 2025. ISSN 2752-106542.

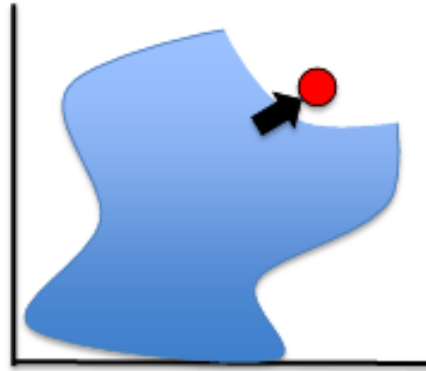


Robust Optimization

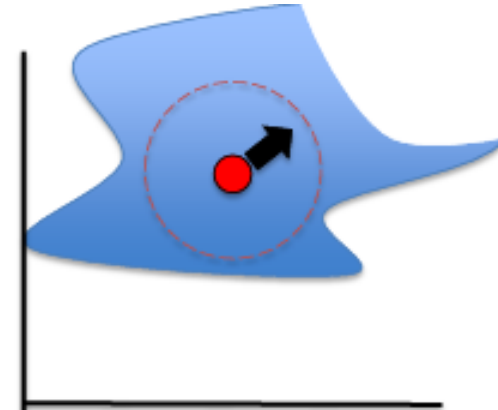
- Decision-making under uncertainty
 - Account for the worst-case



Optimal design



Uncertainty realized



Robust-optimal design

Uncertainty in Agriculture

- What is uncertain?
 - Weather
 - Market prices



Uncertainty in Agriculture

- What is uncertain?
 - ~~Weather~~
 - Market prices



Uncertainty in Agriculture

- What is uncertain?
 - ~~Weather~~
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$$\text{Revenue} = \text{Yield} \times \text{Market price}$$



Modeling CEA Systems

Cetegen & Stuber

- First documented robust optimization approach for CEA systems
- Multiple perspectives
 - Trader's (commodities trader)
 - Modern portfolio theory
 - Grower's (farmer)

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Grower's Model

- Simultaneously find worst-case uncertainty and design and optimize it

$$f^* = \max_{\mathbf{d} \in D, \mathbf{X} \in \Xi} f_{\text{NPV}}(\mathbf{d}, \mathbf{X})$$

$$\text{s.t. } \mathbf{1}^T \mathbf{x}_j = 1, j = 1, \dots, n_p$$

$$d_{z+2} = \left(\sum_{\xi=1}^{\mu} d_{\xi+2} \right) \left(\sum_{i \in \kappa_z} x_{i,j} \right), j = 1, \dots, n_p, z = 1, \dots, \mu$$

$$\mathbf{Qp}_{\min} \leq \left(\sum_{\xi=1}^{\mu} d_{\xi+2} \right) \left(\mathbf{Y} \sum_{j=1}^4 \mathbf{x}_{j+4(q-1)} \right) \leq \mathbf{Qp}_{\max}, q = 1, \dots, n_y$$

$$0 \geq \max_{j \in \{1, \dots, n_p\}} \left\{ \max_{\mathbf{M}_j \in M_j} \mathbf{x}_j^T \mathbf{M}_j \mathbf{x}_j - t_r : \mathbf{M}_j \succeq 0, M_j \in \mathbb{IR}^{n_c \times n_c}, j = 1, \dots, n_p \right\}$$



Grower's Model

- Simultaneously find worst-case uncertainty and design and optimize it

Outer Program

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Inner Program

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Crop allocation
and capacity

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Production limits

$$0 \geq \max_{j \in \{1, \dots, n_p\}} \left\{ \max_{\mathbf{M}_j \in M_j} \mathbf{x}_j^T \mathbf{M}_j \mathbf{x}_j - t_r : \mathbf{M}_j \succeq 0, M_j \in \mathbb{IR}^{n_c \times n_c}, j = 1, \dots, n_p \right\}$$



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Production limits

Multi-period
risk exposure

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Example

- 4 crops



- 25% risk tolerance
- 30-year project horizon

Example

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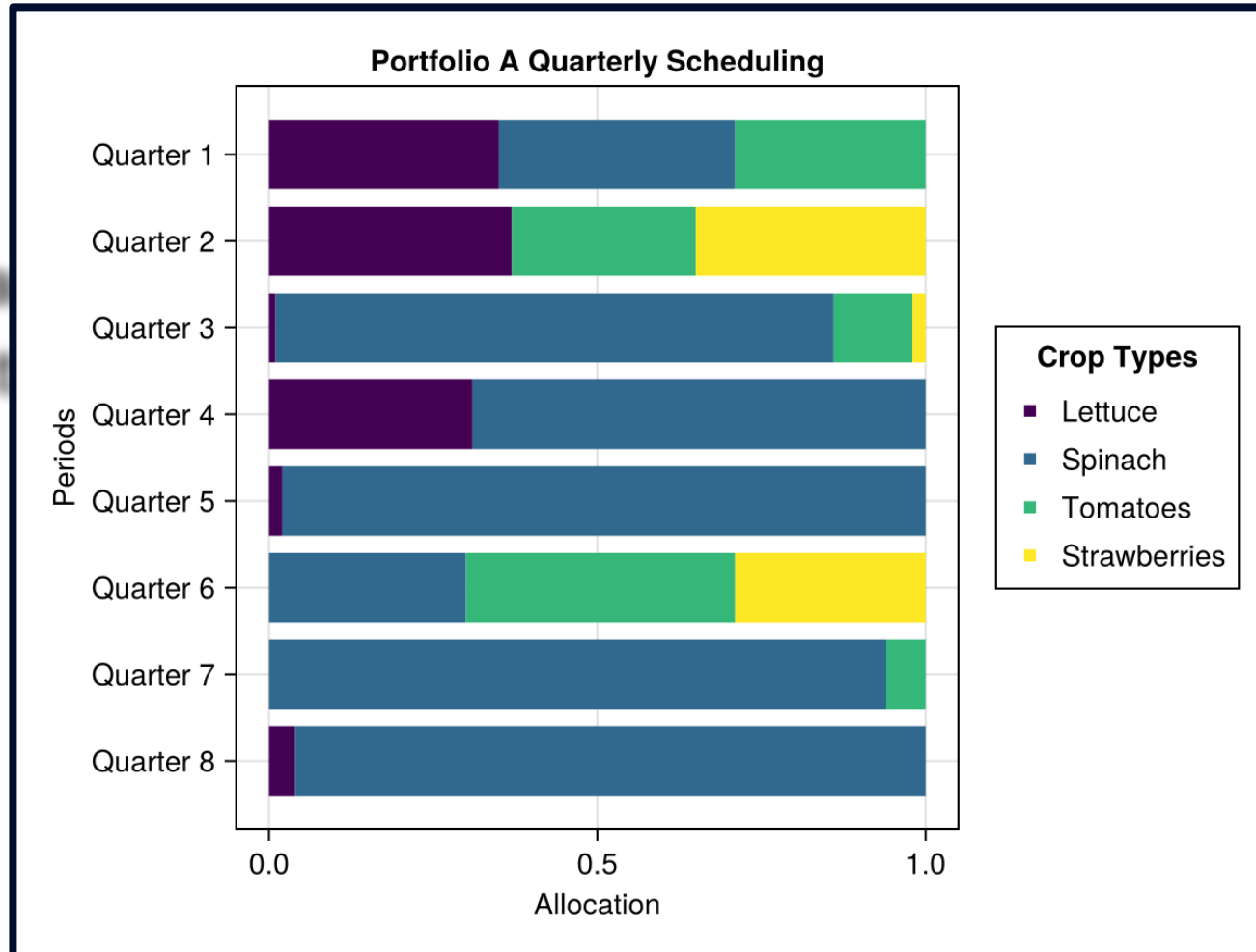
Optimal Capacity	26,672 sq ft.
Optimal NPV	\$21.68 million
Capital Expenses	\$11.5 million
Average Quarterly Operating Expenses	\$5.0 million
Average Quarterly Revenue	\$9.94 million

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Example

- 4 crops
- 25% risk tolerance
- 30-year project

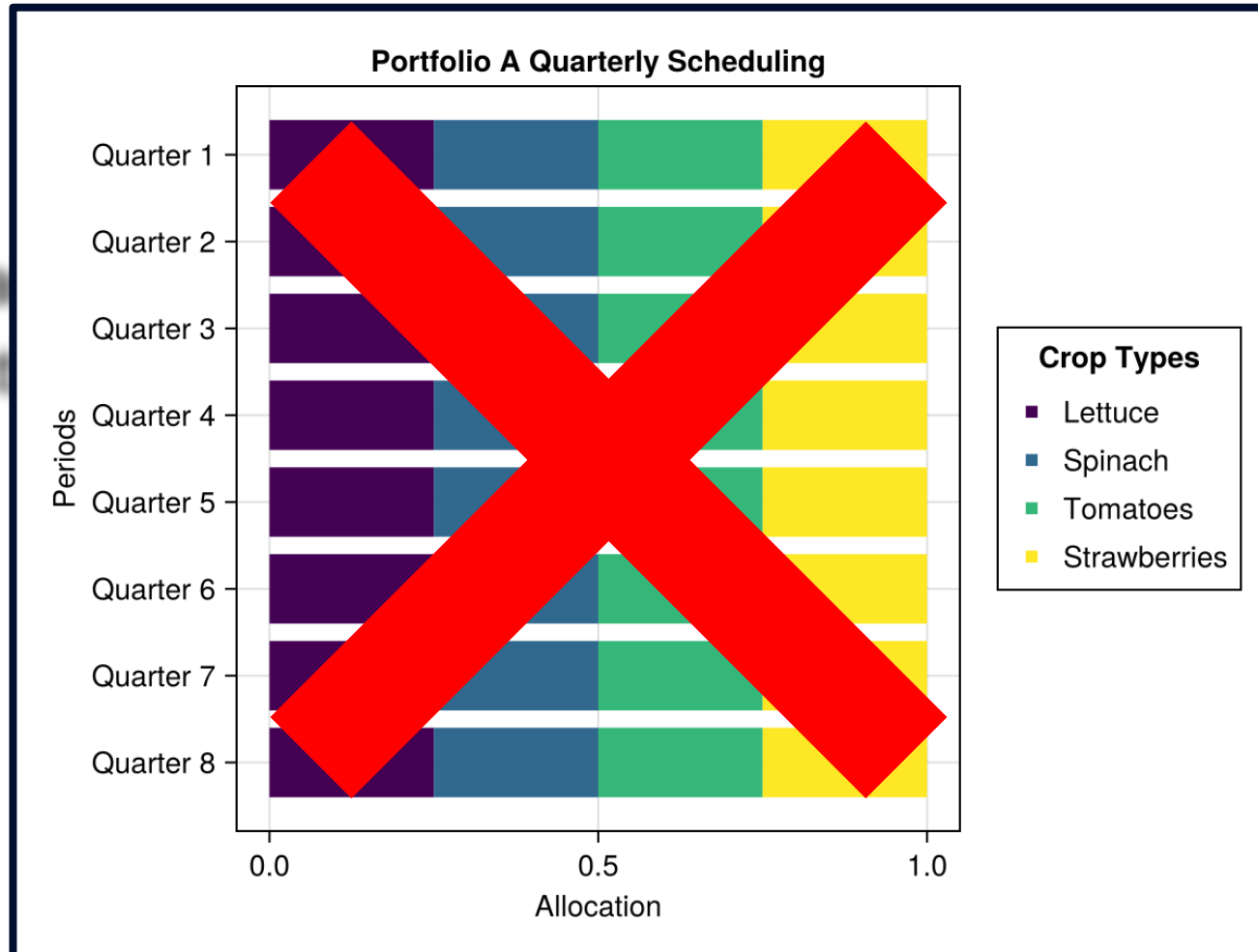


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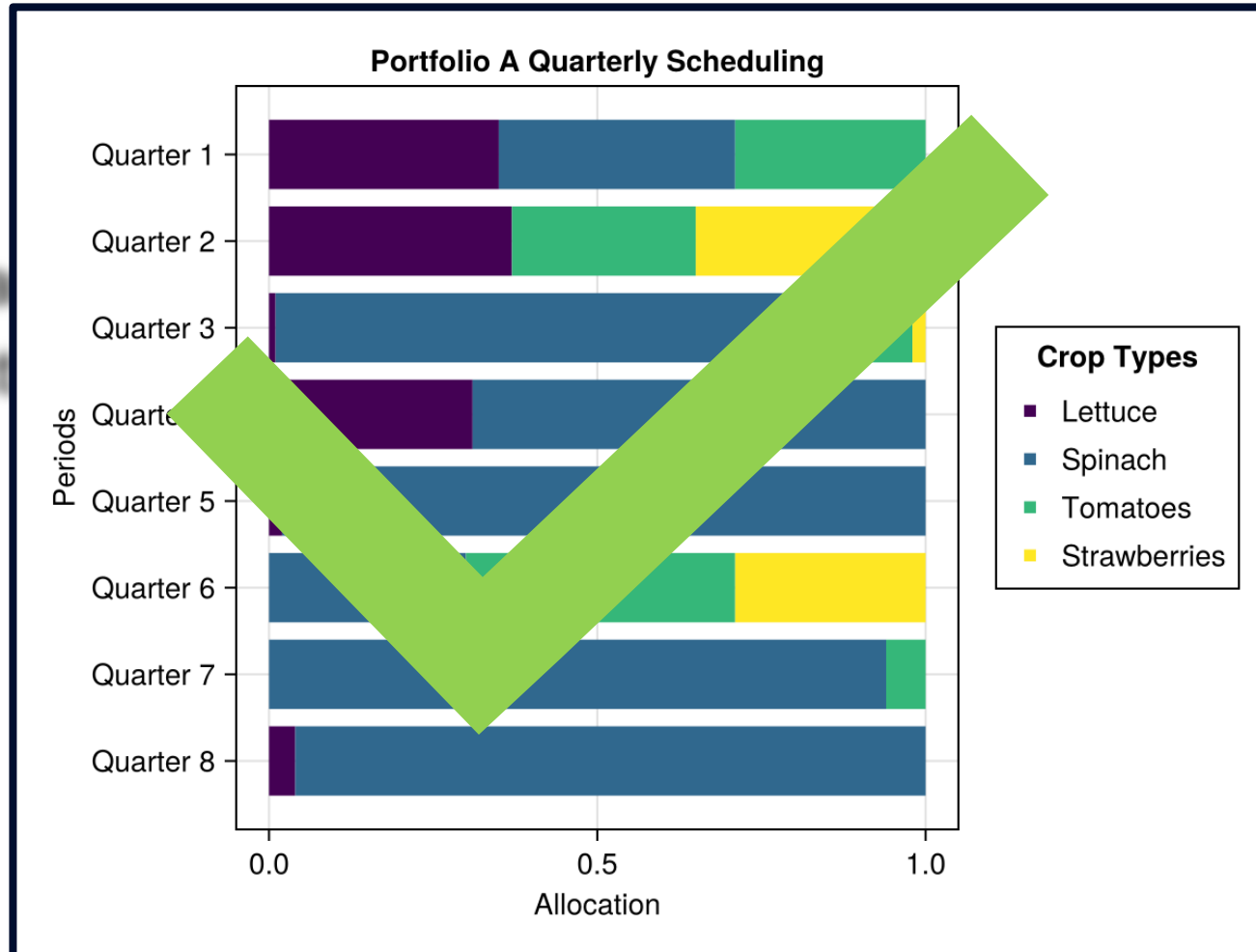
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Improvements

- Develop a more accurate model
 - Adjust grow periods

Crop	Growth Period
Lettuce	3 months
Spinach	3 months
Tomatoes	3 months
Strawberries	3 months



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Spinach	1.5 months
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35 variables → 195 variables

Example Revisited

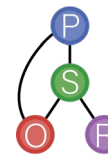
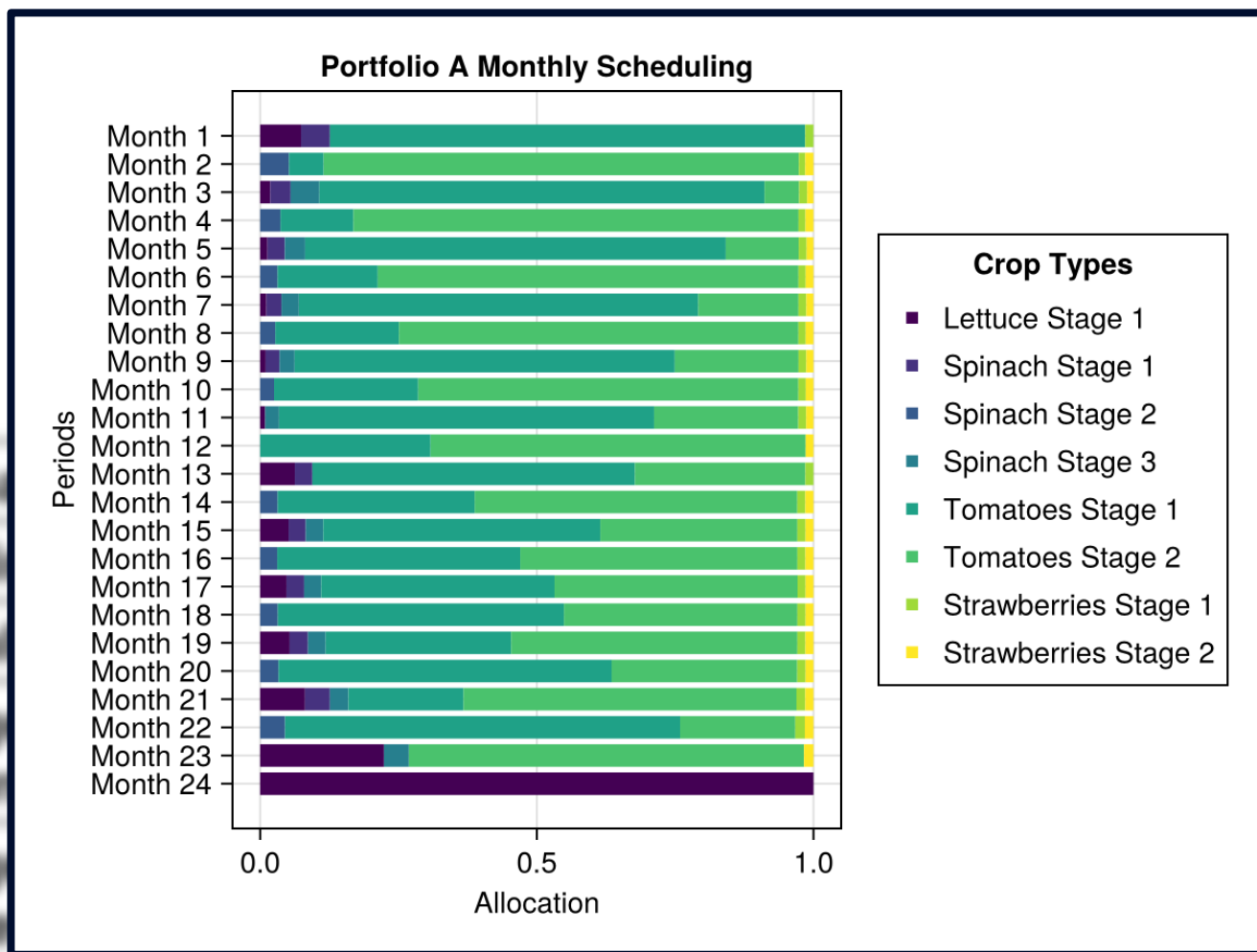
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	Quarterly	Monthly
Optimal Capacity	26,672 sq ft.	70,716 sq ft.
Optimal NPV	\$21.68 million	\$14.5 million
Capital Expenses	\$11.5 million	\$27.7 million
Average Quarterly Operating Expenses	\$5.0 million	\$13.0 million
Average Quarterly Revenue	\$9.94 million	\$20.9 million

Example Revisited

- 4 crops



CEA.jl

- Open-source software tool
- Tunable parameters
 - Number of crops
 - Grow periods
 - Project horizon
 - Tolerable risk
- Efficient
 - Uses current state-of-the-art solvers such as IPOPT, Gurobi, and EAGO



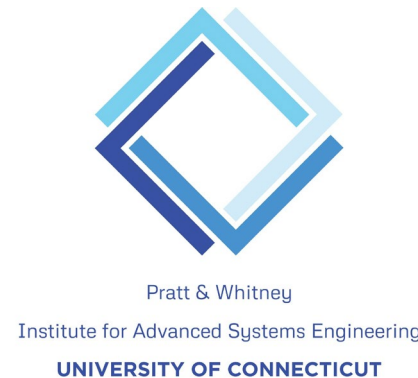
Conclusion

- CEA systems are a good supplement
 - High operating costs
 - Venture risk
- CEA.jl identifies robust-optimal solutions
 - Coming soon
- One step closer to dealing with food insecurity issues



Acknowledgements

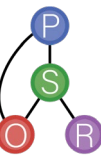
Members of the Process Systems and Operations Research Laboratory at the University of Connecticut (<https://www.psor.uconn.edu>)



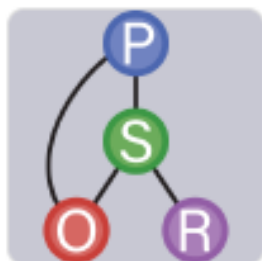
Funding:

John C. Martin Sustainable Engineered Agriculture Project Fund
Pratt & Whitney Endowed Professorship

Any opinions, findings, and conclusions or recommendations expressed in this material are those of the authors and do not necessarily reflect the views of the United States Government.



Questions?



Process Systems and Operations Research Laboratory

The PSOR Laboratory at UConn develops numerical analysis methods and software for process systems engineering applications.

22 followers

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stuber@uconn.edu

<https://psor.uconn.edu>



<https://github.com/PSORLab>

